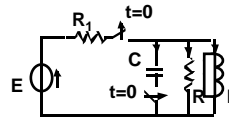


# Lezione 38

E  
s  
e  
r  
c  
i  
z  
i

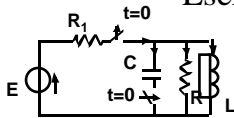
## Esercizi



$$\begin{aligned} R &= R_2 = 1\Omega \\ L &= 4\text{ mH} \\ C &= 1\text{ mF} \\ E &= 2\text{ V} \end{aligned}$$

Il circuito è a regime per  $t < 0$ .

## Esercizi



$$\begin{aligned} R_1 &= R = 1\Omega \\ L &= 4\text{ mH} \\ C &= 1\text{ mF} \\ E &= 2\text{ V} \end{aligned}$$

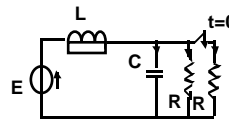
$$i_R = A t e^{-500t} + B e^{-500t}$$

$$v_C(0) = 0 \Rightarrow i_R(0) = 0$$

$$i_L(0) = \frac{E}{R_1} \Rightarrow i_C(0) = -\frac{E}{R_1} \quad i_R = -2 \cdot 10^3 t e^{-500t}$$

$$\left. \frac{di_R}{dt} \right|_{t=0} = \frac{1}{R} \left. \frac{dv_C}{dt} \right|_{t=0} = \frac{-E}{RCR_1}$$

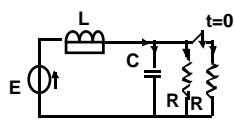
## Esercizi



$$\begin{aligned} R &= 2\Omega \\ L &= 2\text{ mH} \\ C &= 5\text{ mF} \\ E &= 5\text{ V} \end{aligned}$$

Il circuito è a regime per  $t < 0$ .

## Esercizi



$$\begin{aligned} R &= 2\Omega \\ L &= 2\text{ mH} \\ C &= 5\text{ mF} \\ E &= 5\text{ V} \end{aligned}$$

$$i(t) = 5 - 2.5 e^{-100t} \left[ \frac{1}{3} \text{sen}(300t) + \text{cos}(300t) \right]$$

# Lezione 39

E  
s  
e  
r  
c  
i  
z  
i

**Esercizi**

$R_1 = 200 \Omega$   
 $R_2 = 100 \Omega$   
 $L = 100 \text{ mH}$   
 $C = 10 \mu\text{F}$

**Determinare i parametri Y del doppio bipolo**

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 7

**Esercizi**

$R_1 = 200 \Omega$   
 $R_2 = 100 \Omega$   
 $L = 100 \text{ mH}$   
 $C = 10 \mu\text{F}$   
 $\omega = 100 \text{ rad/s}$

$$Y_{11} = \frac{1}{\frac{-L/C}{j(\omega L - 1/\omega C)} + R_1} = 4.99 \cdot 10^{-3} - j2.52 \cdot 10^{-4} \text{ Z}$$

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 8

**Esercizi**

$R_1 = 200 \Omega$   
 $R_2 = 100 \Omega$   
 $L = 100 \text{ mH}$   
 $C = 10 \mu\text{F}$   
 $\omega = 100 \text{ rad/s}$

$$Y_{22} = \frac{R_2 + j \left( \frac{R_1 \omega L}{R_1 + j \omega L} - \frac{1}{\omega C} \right)}{j \left( \frac{R_1 \omega L}{R_1 + j \omega L} - \frac{1}{\omega C} \right) R_2} = 1.00 \cdot 10^{-2} + j2.02 \cdot 10^{-3}$$

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 9

**Esercizi**

$R_1 = 200 \Omega$   
 $R_2 = 100 \Omega$   
 $L = 100 \text{ mH}$   
 $C = 10 \mu\text{F}$   
 $\omega = 100 \text{ rad/s}$

$$Y_{21} = \frac{1}{R_1 + \frac{L/C}{j(\omega L - 1/\omega C)}} \frac{\omega L}{\omega L - 1/\omega C} = 2.02 \cdot 10^{-4} + j4.99 \cdot 10^{-3}$$

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 10

**Esercizi**

$e(t) = 2\sqrt{2} \text{ sen}(100 t) \text{ V}$   
 $i(t) = 3\sqrt{2} \text{ sen}(100 t) \text{ A}$   
 $R_1 = 1 \Omega$   
 $R_2 = 2 \Omega$   
 $L_1 = 10 \text{ mH}$   
 $L_2 = 1 \text{ mH}$   
 $C = 1 \text{ mF}$

$\bar{V}_{R2} = 0.53 + j 0.76$   
 $\bar{I}_{R2} = 0.35 + j 0.35$

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 11

**Esercizi**

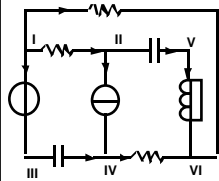
$e(t) = 2\sqrt{2} \text{ sen}(100 t) \text{ V}$   
 $i(t) = 3\sqrt{2} \text{ sen}(100 t) \text{ A}$   
 $R_1 = 1 \Omega$   
 $R_2 = 2 \Omega$   
 $L_1 = 10 \text{ mH}$   
 $L_2 = 1 \text{ mH}$   
 $C = 1 \text{ mF}$

$\bar{V}_{R2} = 0.92\sqrt{2} \text{ sen}(100 t + 0.962)$   
 $\bar{I}_{R1} = 0.50\sqrt{2} \text{ sen}(100 t + 0.791)$

E  
S  
E  
R  
C  
I  
Z  
I

Introduzione ai Circuiti; Esercizi slide n. 12

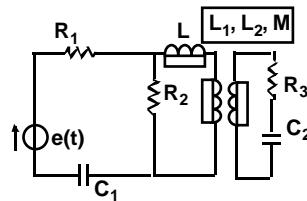
## Multimetro: un circuito con due generatori



$R_{12} = 1,00E+1 \Omega$ ;  $C_{34} = 3,00E-3 F$ ;  $e$   
 $C_{25} = 1,00E-3 F$ ;  $R_{16} = 1,00E+1 \Omega$ ;  $f$   
 $L_{56} = 1,00E-1 H$ ;  $R_{46} = 1,00E+1 \Omega$ ;  $C$   
 $V_{13} = 1,00E+1 V$   $I_{24} = 1,00E+0 A$   $i$   
 $f = 50 Hz$   $Z$   
 $i$



## Esercizi



$e(t) = 10 \sqrt{2} \sin(314 t)$

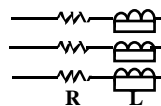
$R_1 = 1 \Omega$   
 $R_2 = 2 \Omega$   
 $R_3 = 4 \Omega$   
 $L = 10 mH$   
 $C_1 = 1 mF$   
 $C_2 = 2 mF$   
 $L_1 = 9 mH$   
 $L_2 = 1 mH$   
 $M = 3 mH$

## Lezione 40

## Esercizi

Terna simmetrica e diretta di tensioni concatenate

$V = 380 v$



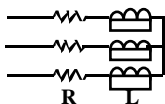
$R = 0.1k \Omega$   
 $L = 100 mH$   
 $\omega = 314 rad/s$

## Esercizi

$Z = 100 + j 31.4 = 104.8 e^{-j0.30}$

$I = 2.1 A$   $P = 1.32 kW$

$V = 380 v$



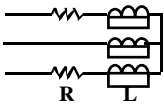
$R = 0.1k \Omega$   
 $L = 100 mH$   
 $\omega = 314 rad/s$

## Lezione 41

## Esercizi

Terna simmetrica e diretta di tensioni concatenate

$$V = 380 \text{ v}$$



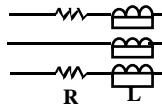
$$\begin{aligned} R &= 0.1 \text{ k} \Omega \\ L &= 100 \text{ mH} \\ \omega &= 314 \text{ rad/s} \end{aligned}$$

E  
s  
e  
r  
c  
i  
z  
i

## Esercizi

$$\bar{V}_{00} = -154 - j 46 \quad \bar{E}_1' = 374 + j 46 \quad \bar{I}_1 = 3.54 + j 0.65$$

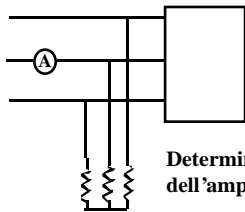
$$V = 380 \text{ v}$$



$$\begin{aligned} R &= 0.1 \text{ k} \Omega \\ L &= 100 \text{ mH} \\ \omega &= 314 \text{ rad/s} \end{aligned}$$

E  
s  
e  
r  
c  
i  
z  
i

## Esercizi

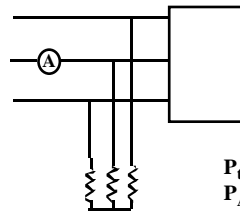


$$\begin{aligned} P &= \sqrt{3} \text{ kW} \\ Q &= 1 \text{ kVAr} \\ R &= 20 \text{ W} \\ V &= 380 \text{ V} \end{aligned}$$

Determinare l'indicazione dell'amperometro

E  
s  
e  
r  
c  
i  
z  
i

## Esercizi

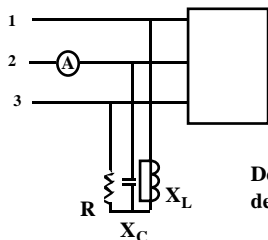


$$\begin{aligned} P &= \sqrt{3} \text{ kW} \\ Q &= 1 \text{ kVAr} \\ R &= 20 \text{ W} \\ V &= 380 \text{ V} \end{aligned}$$

$$\begin{aligned} P_{\text{tot}} &= 8.99 \text{ kW} \\ P_A &= 9.04 \text{ kW} \\ I &= 13.7 \text{ A} \end{aligned}$$

E  
s  
e  
r  
c  
i  
z  
i

## Esercizi

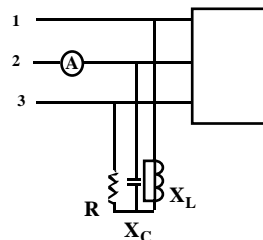


$$\begin{aligned} P &= 1 \text{ kW} \\ Q &= 1 \text{ kVAr} \\ V_{23} &= 300 \text{ V} \\ R &= X_L = X_C = 40 \text{ W} \end{aligned}$$

Determinare l'indicazione dell'amperometro

E  
s  
e  
r  
c  
i  
z  
i

## Esercizi

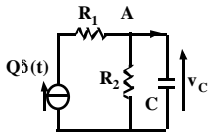


$$\begin{aligned} P &= 1 \text{ kW} \\ Q &= 1 \text{ kVAr} \\ V_{23} &= 300 \text{ V} \\ R &= X_L = X_C = 40 \text{ W} \end{aligned}$$

$$\begin{aligned} \bar{V}_{00'} &= 123.8 e^{-j\pi/6} \\ I &= 4.73 \text{ A} \end{aligned}$$

E  
s  
e  
r  
c  
i  
z  
i

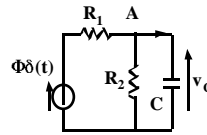
### Qualche esempio



$$v(0^+) = v(0^-) + Q/C$$

**E  
s  
e  
r  
c  
i  
z  
i**

### Qualche esempio

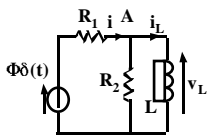


$$i(t) = \Phi \delta(t)/R_1$$

$$v(0^+) = v(0^-) + \Phi/R_1 C$$

**E  
s  
e  
r  
c  
i  
z  
i**

### Qualche esempio



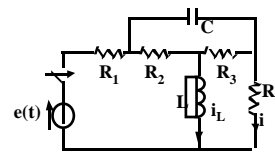
$$i(t) = \Phi \delta(t)/(R_1 + R_2)$$

$$v_L(t) = R_2 \Phi \delta(t)/(R_1 + R_2)$$

$$i_L(0^+) = i_L(0^-) + R_2 \Phi/(R_1 + R_2) L$$

**E  
s  
e  
r  
c  
i  
z  
i**

### Un esempio



$$R_1 = R_4 = 5 \Omega;$$

$$R_2 = R_3 = 0.5 \Omega;$$

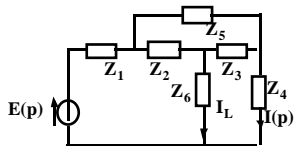
$$L = 1 \text{ H};$$

$$C = 0.5 \text{ F};$$

$$e(t) = 10 \text{ sen}(4t).$$

**E  
s  
e  
r  
c  
i  
z  
i**

### Un esempio



$$Z_1 = Z_4 = 5;$$

$$Z_2 = Z_3 = 0.5;$$

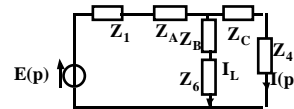
$$Z_6 = p;$$

$$Z_5 = 2/p;$$

$$E(p) = 40/(p^2 + 16)$$

**E  
s  
e  
r  
c  
i  
z  
i**

### Un esempio



$$Z_1 = Z_4 = 5;$$

$$Z_2 = Z_3 = 0.5;$$

$$Z_6 = p;$$

$$Z_5 = 2/p;$$

$$E(p) = 40/(p^2 + 16)$$

$$Z_A = \frac{1}{p+2} \quad Z_B = \frac{0.25 p}{p+2} \quad Z_C = \frac{1}{p+2}$$

**E  
s  
e  
r  
c  
i  
z  
i**

Un esempio

**E**  
**s**  
**e**  
**r**  
**c**  
**z**

$Z_1 = Z_4 = 5;$   
 $Z_2 = Z_3 = 0.5;$   
 $Z_6 = p;$   
 $Z_5 = 2/p;$   
 $E(p) = 40/(p^2 + 16)$

$$I(p) = \frac{Z_B + p}{Z_B + Z_C + 5 + p} \frac{E(p)}{5 + Z_A + \frac{(Z_B + p)(Z_C + 1)}{Z_B + p + Z_C + 5}}$$

Introduzione ai Circuiti; Esecizi slide n. 31

Un esempio

**E**  
**s**  
**e**  
**r**  
**c**  
**z**  
**i**

$Z_1 = Z_4 = 5;$   
 $Z_2 = Z_3 = 0.5;$   
 $Z_6 = p;$   
 $Z_5 = 2/p;$   
 $E(p) = 40/(p^2 + 16)$

$$I(p) = \frac{40}{p^2 + 16} \frac{p + 2,25}{5p + 11} \frac{p + 2}{2p^2 + 9,5p + 11}$$

Introduzione ai Circuiti; Esecizi slide n. 32

Un esempio

$p = -2$   
 $p = -11/4$

$2p^2 + 9,5p + 11 = 2(p + 2)(p + \frac{11}{4})$

$$I(p) = \frac{40}{p^2 + 16} \frac{p + 2,25}{5p + 11} \frac{p + 2}{2p^2 + 9,5p + 11}$$

**E**  
**s**  
**e**  
**r**  
**c**  
**z**  
**i**

Introduzione ai Circuiti; Esecizi slide n. 33

Un esempio

$p = -2$   
 $p = -11/4$

$2p^2 + 9,5p + 11 = 2(p + 2)(p + \frac{11}{4})$

$$I(p) = \frac{4}{p^2 + 16} \frac{p + 2,25}{p + \frac{11}{5}} \frac{1}{p + \frac{11}{4}}$$

**E**  
**s**  
**e**  
**r**  
**c**  
**z**  
**i**

Introduzione ai Circuiti; Esecizi slide n. 34

Un esempio

$p = -2$   
 $p = -11/4$

$2p^2 + 9,5p + 11 = 2(p + 2)(p + \frac{11}{4})$

$$I(p) = \frac{Ap + B}{p^2 + 16} + \frac{C}{p + \frac{11}{5}} + \frac{D}{p + \frac{11}{4}}$$

**E**  
**s**  
**e**  
**r**  
**c**  
**z**  
**i**

Introduzione ai Circuiti; Esecizi slide n. 35

Un esempio

$e^{-\alpha t} \Rightarrow \frac{1}{p + \alpha}$

$\cos \beta t \Rightarrow \frac{p}{p^2 + \beta^2}$

$\sin \beta t \Rightarrow \frac{\beta}{p^2 + \beta^2}$

**E**  
**s**  
**e**  
**r**  
**c**  
**z**  
**i**

$$I(p) = \frac{Ap + B}{p^2 + 16} + \frac{C}{p + \frac{11}{5}} + \frac{D}{p + \frac{11}{4}}$$

Introduzione ai Circuiti; Esecizi slide n. 36

### Un esempio

$$e^{-\alpha t} \Rightarrow \frac{1}{p+\alpha}$$

$$\cos \beta t \Rightarrow \frac{p}{p^2+\beta^2}$$

$$\sin \beta t \Rightarrow \frac{\beta}{p^2+\beta^2}$$

$$i(t) = L^{-1}\{I_1(p) + I_2(p)\} = A \cos 4t + \frac{B}{4} \sin 4t + C e^{(11/5)t} + (D - 1) e^{(11/4)t}$$

**E  
s  
e  
m  
p  
l  
o**